

THE HISTORY | OF | MATHEMATICS



Mathematics and the Laws of Nature

Revised Edition

Developing the Language of Science



JOHN TABAK, PH.D.

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THE LAWS OF NATURE**

Revised Edition



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MATHEMATICS AND THE LAWS OF NATURE: Developing the Language of Science, Revised Edition

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Facts On File, Inc.
An imprint of Infobase Learning
132 West 31st Street
New York NY 10001

Library of Congress Cataloging-in-Publication Data

Tabak, John.

Mathematics and the laws of nature : developing the language of science / John Tabak—Rev. ed.

p. cm.—(The history of mathematics)

Includes bibliographical references and index.

ISBN 978-0-8160-7943-8 (alk. paper)

ISBN 978-1-4381-3624-0 (e-book)

1. Mathematics—History. 2. Science—History. I. Title.

QA21.T22 2011

510.9—dc22 2010021599

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Text design by David Strelecky

Composition by Hermitage Publishing Services

Illustrations by Dale Williams

Photo research by Elizabeth H. Oakes

Cover printed by Yurchak Printing, Inc., Landisville, Pa.

Book printed and bound by Yurchak Printing, Inc., Landisville, Pa.

Date printed: May 2011

Printed in the United States of America

10 9 8 7 6 5 4 3 2 1

This book is printed on acid-free paper.

To George Baker: He is a law unto himself.

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